St Margaret Clitherow Calculation Policy Graphical user interface, website

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Ourcalculation policy

The following pages show the progression in calculation (addition, subtraction, multiplication and division) and how this works in line with the National Curriculum. The consistent use of the CPA (concrete, pictorial, abstract) helps children develop mastery across all the operations in an efficient and reliable way. This policy shows how these methods develop children’s confidence in their understanding of both written and mental methods.

**EYFS**

In Reception, children focus on concrete and pictorial representations. At this stage, children focus on representing objects in different ways e.g. understanding that 5 cars can also be represented as 5 counters, 5 cubes, 5 pictures of cars, etc.

In Reception, children are encouraged to record their findings in their own way. This may include writing number sentences e.g. 3 + 4 = 7, however this is not a requirement until Year 1.

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| ***Priory* calculation policy Reception** |
| Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. Children record their calculations in their own ways, there is no expectation of number sentences at this stage, however children may choose this way to record their thinking. |
| Key language: count, forwards, backwards, whole, part, recombine, break apart, ones, ten, tens, number bond, add, adding together, addition, plus, total, altogether, first, then, now, subtract, subtraction, find the difference, take away, minus, left, less, more, fewer, group, share, equal, equals, is equal to, groups, equal groups, divide, share, shared equally |

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| Progression in calculation in Reception | | |
| Addition:  Children start to explore addition by sorting groups. They then use sorting to develop their understanding of parts and wholes.  Children combine groups to find the whole, using a part-whole model to support their thinking. They also use the part-whole model to find number bonds within and to 10.  Using a five frame and ten frame, children add by counting on. They start by finding one more before adding larger numbers using counters or cubes on the frames.  Children use a number track to add by counting on. Linking this learning to playing board games is an effective way to support children’s addition. | Subtraction:  Children start to explore subtraction by sorting groups. They use sorting to develop their understanding of parts and wholes.  When comparing groups, children use the language more than and fewer than. This will lead to finding the difference when they move into KS1.  Children then connect subtraction with the idea of counting back and finding one less using a five frame to support their thinking.  They explore subtraction by breaking apart a whole to find a missing part. This links to their developing recall of number bonds.  Children count back within 20 using number tracks and ten frames to see the effect of taking away. | Multiplication and Division:  Children first start to look at the idea of equal groups through their exploration of doubles. They use five frames and objects to check that groups are equal.  Children then explore halving numbers by making two equal groups. They highlight patterns between doubling and halving seeing that double 2 is 4 and half of 4 is 2.  As well as halving, children also explore sharing into more than two equal groups. They share objects one by one, ensuring that each group has an equal share. |

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| Reception | | |
|  | **Real-life representation** | **Other representations** |
| **Addition** | **Counting and adding more (within 5)**  Children add one more person or object to a group to find one more.    One more than 3 is 4. | **Counting and adding more (within 5)**  Children represent first, then, now stories on a five frame. They make the first number and then add one more.    *First, there are 3 bikes.*  *Then, 1 more bike came.*  *Now, there are 4 bikes.* |

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|  | Combining groups to find the whole  Children sort people and objects into parts and combine them to find the whole.  ../COLLATIONS%200609/wetransfer-687268/SBN6105_U09_AW_004.jpg  *The parts are 3 and 4. The whole is 7.* | Combining groups to find the whole  Children use counters or cubes in a part-whole model to find the whole.    The parts are 3 and 4. The whole is 7. |

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|  | Finding number bonds to 10  Children combine two groups to find a number bond to 10.    *There are 8 bottles on the wall.*  *There are 2 bottles on the floor.*  *There are 10 bottles altogether.* | Finding number bonds to 10  Use ten frames and part-whole models to represent key number bonds.    *8 and 2 is 10.*  *There are 10 altogether.*    *6 and 4 is 10.*  *There are 10 altogether.* |

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|  | Adding by counting on (number track)  Children jump along a physical number track. They start at the larger number and count on the smaller number to find the total.  ../COLLATIONS%200609/wetransfer-687268/SBN6105_U13_AW_002.ai | Adding by counting on (number track)  Children use a number track and a counter. They start at the larger number and count on the smaller number to find the total. |
|  | **Adding by counting on (ten frames)**  Children find the total number by counting on from the larger number.  **../COLLATIONS%200609/wetransfer-687268/SBN6105_U14_AW_012.ai** | **Adding by counting on (ten frames)**  Children make the larger number on the ten frames and then make the smaller number, counting on to find the total. They can use counters, cubes or other objects on the ten frames. |
|  | **Sorting groups (optional)**  Children sort everyday objects into groups.  ../COLLATIONS%200609/wetransfer-687268/PMR_TermA_FC_U2_W4_Discover_aw03%20new.jpg |  |

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| Subtraction | Comparing groups  Children line up objects to compare the amount. They line the objects up either horizontally or vertically.  ../COLLATIONS%200609/wetransfer-687268/PMR_TermA_FC_U3_W5_Discover_aw04.jpg  *Ella has more conkers.*  *Tom has fewer conkers.* | Comparing groups  Children line up cubes or counters to compare the amount in each group. Lines can either be horizontal or vertical. A starting line helps to line the objects accurately.    *There are more yellow cubes.*  *There are fewer red cubes.* |

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|  | Counting back and taking away (within 5)  Children remove one more person or object from a group to find one less.    *First, there were 3 children.*  *Then, 1 child left.*  *Now, there are 2 children.* | Counting back and taking away (within 5)  Children use five frames and objects to make a number. They then remove or cross out one object to find one less.    *One less than 3 is 2.* |

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|  | Introducing the part-whole model  Children sort everyday objects into parts.      *One part is the*    *The other part is the* | Introducing the part-whole model  Children use counters or cubes to represent objects in a part-whole model.    *The whole is 5.*  *2 is a part.*  *3 is a part.* |
|  | **Finding number bonds to 10**  Children partition 10 into different groups to find the number bonds to 10.    Children begin to work with subtraction number bonds. They break apart 10 to identify different number bonds to 10**.**  A picture containing diagram  Description automatically generated  *10 are bouncing.*  *2 get off.*  *8 are left.*  *10 – 2 = 8* | **Finding number bonds to 10**  Children use part-whole models, ten frames and counters to find the number bonds to 10.    *10 is the whole.*  *5 is a part and 5 is a part.*    *10 is the whole.*  *5 is a part and 5 is a part.*  Children use part-whole models, and counters to find missing parts and the subtraction number bonds to 10.  Diagram, shape  Description automatically generated  *The parts are 8 and 2.*  *10 is the whole.* |
|  | **Counting back and taking away (number track)**  Children use game boards and human number tracks to subtract by counting back.    *9 take away 3 equals 6*  *9…8…7…6* | **Counting back and taking away (number track)**  Children use a number track and a counter. They start at the larger number and count back the smaller number to find the answer.    *9 take away 3 equals 6*  *9…8…7…6* |
|  | **Counting back and taking away (ten frames)**  Children count backwards to find one less with numbers up to 20.  *One less than 16 is 15.* | **Counting back and taking away (ten frames)**  Children remove counters from ten frames to support in counting back with numbers up to 20.    *One less than 16 is 15.* |
|  | **Sorting groups (optional)**  Children sort everyday objects into groups.  ../COLLATIONS%200609/wetransfer-687268/PMR_TermA_FC_U2_W4_Discover_aw03%20new.jpg |  |
| **Multiplication** | **Making doubles**  Children explore doubles in their environment including in games such as on dominoes or dice. They focus on the understanding of doubles being 2 equal groups.    *Double 4 is 8.*  *Double 2 is 4.*  *Double 3 is 6.* | **Making doubles**  Children use five frames to find doubles by lining up counters or cubes.    *Double 4 is 8.* |
| **Division** | **Halving and sharing**  Children explore halving and sharing through practical sharing using real life scenarios including sharing fruit or classroom equipment.    *Half of 8 is 4.* | **Halving and sharing**  Children use five frames to share amounts fairly and to check that the groups are equal. They share the counters/cubes one by one.    *Half of 6 is 3.* |

KS1

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| **KEY STAGE 1** |
| Children develop the core ideas that underpin all calculation. They begin by connecting calculation with counting on and counting back, but they should learn that understanding wholes and parts will enable them to calculate efficiently and accurately, and with greater flexibility. They learn how to use an understanding of 10s and 1s to develop their calculation strategies, especially in addition and subtraction. |
| Key language: whole, part, ones, ten, tens, number bond, add, addition, plus, total, altogether, subtract, subtraction, find the difference, take away, minus, less, more, group, share, equal, equals, is equal to, groups, equal groups, times, multiply, multiplied by, divide, share, shared equally, times-table |

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| Progression in calculation in Key Stage 1 | | | | | |
| Addition and subtraction: Children first learn to connect addition and subtraction with counting, but they soon develop two very important skills: an understanding of parts and wholes, and an understanding of unitising 10s, to develop efficient and effective calculation strategies based on known number bonds and an increasing awareness of place value. Addition and subtraction are taught in a way that is interlinked to highlight the link between the two operations.  A key idea is that children will select methods and approaches based on their number sense. For example, in Year 1, when faced with 15 − 3 and 15 − 13, they will adapt their ways of approaching the calculation appropriately. The teaching should always emphasise the importance of mathematical thinking to ensure accuracy and flexibility of approach, and the importance of using known number facts to harness their recall of bonds within 20 to support both addition and subtraction methods.  In Year 2, they will start to see calculations presented in a column format, although this is not expected to be formalised until KS2. The column method in Year 2 as an option; depending on the needs of the child, this may not be introduced until Year 3. | | Multiplication and division: Children develop an awareness of equal groups and link this with counting in equal steps, starting with 2s, 5s and 10s. In Year 2, they learn to connect the language of equal groups with the mathematical symbols for multiplication and division.  They learn how multiplication and division can be related to repeated addition and repeated subtraction to find the answer to the calculation.  In this key stage, it is vital that children explore and experience a variety of strong images and manipulative representations of equal groups, including concrete experiences as well as abstract calculations.  Children begin to recall some key multiplication facts, including doubles, and an understanding of the 2, 5 and 10 times-tables and how they are related to counting. | | Fractions: In Year 1, children encounter halves and quarters, and link this with their understanding of sharing. They experience key spatial representations of these fractions, and learn to recognise examples and non-examples, based on their awareness of equal parts of a whole.  In Year 2, they develop an awareness of unit fractions and experience non-unit fractions, and they learn to write them and read them in the common format of numerator and denominator. | |
| Year 1 | | | | | |
|  | **Concrete** | | **Pictorial** | | **Abstract** |
| **Year 1**  **Addition** | **Counting and adding more**  Children add one more person or object to a group to find one more. | | **Counting and adding more**  Children add one more cube or counter to a group to represent one more.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_001.jpg  *One more than 4 is 5.* | | **Counting and adding more**  Use a number line to understand how to link counting on with finding one more.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_002.jpg  *One more than 6 is 7.*  *7 is one more than 6.*  Learn to link counting on with adding more than one.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_003.jpg  *5 + 3 = 8* |
| Understanding part-part-whole relationship  Sort people and objects into parts and understand the relationship with the whole.  A picture containing text, clipart, doll  Description automatically generated  *The parts are 2 and 4. The whole is 6.* | | **Understanding part-part-whole relationship**  Children draw to represent the parts and understand the relationship with the whole.  Icon  Description automatically generated  *The parts are 1 and 5. The whole is 6.* | | **Understanding part-part-whole relationship**  Use a part-whole model to represent the numbers.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_006.jpg  6 + 4 = 10 |
|  | **Knowing and finding number bonds within 10**  Break apart a group and put back together to find and form number bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_007.jpg  *3 + 4 = 7*    *6 = 2 + 4* | | **Knowing and finding number bonds within 10**  Use five and ten frames to represent key number bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_009.jpg  *5 = 4 + 1*  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_010.jpg  *10 = 7 + 3* | | **Knowing and finding number bonds within 10**  Use a part-whole model alongside other representations to find number bonds. Make sure to include examples where one of the parts is zero.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_011.jpg  *4 + 0 = 4*  *3 + 1 = 4* |
| **Understanding teen numbers as a complete 10 and some more**  Complete a group of 10 objects and count more.  A picture containing text, writing implement, stationary, pen  Description automatically generated  *13 is 10 and 3 more.* | | **Understanding teen numbers as a complete 10 and some more**  Use a ten frame to support understanding of a complete 10 for teen numbers.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_013.jpg  *13 is 10 and 3 more.* | | **Understanding teen numbers as a complete 10 and some more**.  *1 ten and 3 ones equal 13.*  *10 + 3 = 13* |
|  | **Adding by counting on**  Children use knowledge of counting to 20 to find a total by counting on using people or objects.  A picture containing text, clipart  Description automatically generated | | **Adding by counting on**  Children use counters to support and represent their counting on strategy.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_015.jpg | | **Adding by counting on**  Children use number lines or number tracks to support their counting on strategy.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_016.jpg |
| **Adding the 1s**  Children use bead strings to recognise how to add the 1s to find the total efficiently.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_017.jpg  *2 + 3 = 5*  *12 + 3 = 15* | | **Adding the 1s**  Children represent calculations using ten frames to add a teen and 1s.  A picture containing text, building, window, clipart  Description automatically generated  *2 + 3 = 5*  *12 + 3 = 15* | | **Adding the 1s**  Children recognise that a teen is made from a 10 and some 1s and use their knowledge of addition within 10 to work efficiently.  *3 + 5 = 8*  *So, 13 + 5 = 18* |
| **Bridging the 10 using number bonds**  Children use a bead string to complete a 10 and understand how this relates to the addition.    *7 add 3 makes 10.*  *So, 7 add 5 is 10 and 2 more.* | | **Bridging the 10 using number bonds**  Children use counters to complete a ten frame and understand how they can add using knowledge of number bonds to 10.  Diagram, shape  Description automatically generated  . | | **Bridging the 10 using number bonds**  Use a part-whole model and a number line to support the calculation.  Diagram  Description automatically generated with low confidence  *9 + 4 = 13* |
| **Year 1**  **Subtraction** | **Counting back and taking away**  Children arrange objects and remove to find how many are left.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_022.jpg  *1 less than 6 is 5.*  *6 subtract 1 is 5*. | | **Counting back and taking away**  Children draw and cross out or use counters to represent objects from a problem.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_023.jpg | | **Counting back and taking away**  Children count back to take away and use a number line or number track to support the method.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_024.jpg  *9 − 3 = 6* |
| **Finding a missing part, given a whole and a part**  Children separate a whole into parts and understand how one part can be found by subtraction.    *8 − 5 = ?* | | **Finding a missing part, given a whole and a part**  Children represent a whole and a part and understand how to find the missing part by subtraction.  A picture containing text, clipart, clock  Description automatically generated | | **Finding a missing part, given a whole and a part**  Children use a part-whole model to support the subtraction to find a missing part.  A picture containing text, clipart  Description automatically generated  *7 − 3 = ?*  Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model. |
| **Finding the difference**  Arrange two groups so that the difference between the groups can be worked out.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_029.jpg  *8 is 2 more than 6.*  *6 is 2 less than 8.*  *The difference between 8 and 6 is 2.* | | **Finding the difference**  Represent objects using sketches or counters to support finding the difference.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_030.jpg  *5 − 4 = 1*  *The difference between 5 and 4 is 1.* | | **Finding the difference**  Children understand ‘find the difference’ as subtraction.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_031.jpg  *10 − 4 = 6*  *The difference between 10 and 6 is* *4.* |
| **Subtraction within 20**  Understand when and how to subtract 1s efficiently.  Use a bead string to subtract 1s efficiently.    *5 − 3 = 2*  *15 − 3 = 12* | | **Subtraction within 20**  Understand when and how to subtract 1s efficiently.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_033.jpg  *5 − 3 = 2*  *15 − 3 = 12* | | **Subtraction within 20**  Understand how to use knowledge of bonds within 10 to subtract efficiently.  *5 − 3 = 2*  *15 − 3 = 12* |
| **Subtracting 10s and 1s**  For example: 18 − 12  Subtract 12 by first subtracting the 10, then the remaining 2.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_034.jpg  *First subtract the 10, then take away 2.* | | **Subtracting 10s and 1s**  For example: 18 − 12  Use ten frames to represent the efficient method of subtracting 12.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_035.jpg  *First subtract the 10, then subtract 2.* | | **Subtracting 10s and 1s**  Use a part-whole model to support the calculation.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_036.jpg  *19 − 14*  *19 − 10 = 9*  *9 − 4 = 5*  *So, 19 − 14 = 5* |
|  | **Subtraction bridging 10 using number bonds**  For example: 12 − 7  Arrange objects into a 10 and some 1s, then decide on how to split the 7 into parts.  A picture containing text, building, window  Description automatically generated  *7 is 2 and 5, so I take away the 2 and  then the 5.* | | **Subtraction bridging 10 using number bonds**  Represent the use of bonds using ten frames.  A picture containing building, window, cosmetic  Description automatically generated  *For 13 – 5, I take away 3 to make 10, then take away 2 to make 8.* | | **Subtraction bridging 10 using number bonds**  Use a number line and a part-whole model to support the method.  13 − 5  A picture containing diagram  Description automatically generated |
| **Year 1**  **Multiplication** | **Recognising and making equal groups**  Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.  A group of cupcakes with pink frosting  Description automatically generated with low confidence | | **Recognising and making equal groups**  Children draw and represent equal and unequal groups.  Shape  Description automatically generated | | **Describe equal groups using words**  *Three equal groups of 4*.  *Four equal groups of 3*. |
| **Finding the total of equal groups by counting in 2s, 5s and 10s**  Shape, arrow  Description automatically generated  There are 5 pens in each pack …  5…10…15…20…25…30…35…40… | | **Finding the total of equal groups by counting in 2s, 5s and 10s**  100 squares and ten frames support counting in 2s, 5s and 10s.  Calendar  Description automatically generated | | **Finding the total of equal groups by counting in 2s, 5s and 10s**  Use a number line to support repeated addition through counting in 2s, 5s and 10s.  A picture containing shape  Description automatically generated |
| **Year 1**  **Division** | **Grouping**  Learn to make equal groups from a whole and find how many equal groups of a certain size can be made.  Sort a whole set people and objects into equal groups.  A group of children  Description automatically generated with low confidence  *There are 10 children altogether.*  *There are 2 in each group.*  *There are 5 groups.* | | **Grouping**  Represent a whole and work out how many equal groups.  A picture containing text, clipart  Description automatically generated  *There are 10 in total.*  *There are 5 in each group.*  *There are 2 groups.* | | **Grouping**  Children may relate this to counting back in steps of 2, 5 or 10.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_046.jpg |
| **Sharing**  Share a set of objects into equal parts and work out how many are in each part**.**  Diagram  Description automatically generated | | **Sharing**  Sketch or draw to represent sharing into equal parts. This may be related to fractions. | | **Sharing**  *10 shared into 2 equal groups gives 5 in each group.* |

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| Year 2 | | | |
|  | **Concrete** | **Pictorial** | **Abstract** |
| **Year 2**  **Addition** |  |  |  |
| **Understanding 10s and 1s** | Group objects into 10s and 1s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_050.jpg  Bundle straws to understand unitising of 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_051.jpg | Understand 10s and 1s equipment, and link with visual representations on ten frames.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_052.jpg | Represent numbers on a place value grid, using equipment or numerals.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_053.jpg  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_054.jpg |
| **Adding 10s** | Use known bonds and unitising to add 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_055.jpg  *I know that 4 + 3 = 7.  So, I know that 4 tens add 3 tens is 7 tens.* | Use known bonds and unitising to add 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_056.jpg  *I know that 4 + 3 = 7.  So, I know that 4 tens add 3 tens is 7 tens.* | Use known bonds and unitising to add 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_057.jpg  *4 + 3 = 7*  *4 tens + 3 tens = 7 tens*  *40 + 30 = 70* |
| **Adding a  1-digit number to a 2-digit number not bridging a 10** | Add the 1s to find the total. Use known bonds within 10.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_058.jpg  *41 is 4 tens and 1 one.*  *41 add 6 ones is 4 tens and 7 ones.*  This can also be done in a place value grid.  Shape, square  Description automatically generated | Add the 1s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_059.jpg  *34 is 3 tens and 4 ones.*  *4 ones and 5 ones are 9 ones.*  *The total is 3 tens and 9 ones.*  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_061.jpg | Add the 1s.  Understand the link between counting on and using known number facts. Children should be encouraged to use known number bonds to improve efficiency and accuracy.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_062.jpg  This can be represented horizontally or vertically.  *34 + 5 = 39*  *or*  *C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_063.jpg* |
| **Adding a  1-digit number to a 2-digit number bridging 10** | Complete a 10 using number bonds.  A group of red chairs  Description automatically generated with medium confidence  *There are 4 tens and 5 ones.*  *I need to add 7. I will use 5 to complete a 10, then add 2 more.* | Complete a 10 using number bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_065.jpg | Complete a 10 using number bonds.  Diagram  Description automatically generated  *7 = 5 + 2*  *45 + 5 + 2 = 52* |
| **Adding a  1-digit number to a 2-digit number using exchange** | Exchange 10 ones for 1 ten.  Diagram, schematic  Description automatically generated | Exchange 10 ones for 1 ten.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_068.jpg | Exchange 10 ones for 1 ten.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_069.jpg |
| **Adding a multiple of 10 to a 2-digit number** | Add the 10s and then recombine.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_070.jpg  *27 is 2 tens and 7 ones.*  *50 is 5 tens.*  *There are 7 tens in total and 7 ones.*  *So, 27 + 50 is 7 tens and 7 ones.* | Add the 10s and then recombine.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_071.jpg  *66 is 6 tens and 6 ones.*  *66 + 10 = 76*  A 100 square can support this understanding.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_072.jpg | Add the 10s and then recombine.  *37 + 20 = ?*  *30 + 20 = 50*  *50 + 7 = 57*  *37 + 20 = 57* |
| **Adding a multiple of 10 to a 2-digit number using columns** | Add the 10s using a place value grid to support.  Diagram  Description automatically generated  *16 is 1 ten and 6 ones.*  *30 is 3 tens.*  *There are 4 tens and 6 ones in total.* | Add the 10s using a place value grid to support.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_074.jpg  *16 is 1 ten and 6 ones.*  *30 is 3 tens.*  *There are 4 tens and 6 ones in total.* | Add the 10s represented vertically. Children must understand how the method relates to unitising of 10s and place value.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_075.jpg  *1 + 3 = 4*  *1 ten + 3 tens = 4 tens*  *16 + 30 = 46* |
| **Adding two  2-digit numbers** | Add the 10s and 1s separately.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_076.jpg  *5 + 3 = 8*  *There are 8 ones in total.*  *3 + 2 = 5*  *There are 5 tens in total.*  *35 + 23 = 58* | Add the 10s and 1s separately. Use a  part-whole model to support.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_077.jpg  *11 = 10 + 1*  *32 + 10 = 42*  *42 + 1 = 43*  *32 + 11 = 43* | Add the 10s and the 1s separately, bridging 10s where required. A number line can support the calculations.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_078.jpg  *17 + 25* |
| **Adding two  2-digit numbers using a place value grid** | Add the 1s. Then add the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_079.jpg |  | Add the 1s. Then add the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_080.jpg |
| **Adding two  2-digit numbers with exchange** | Add the 1s. Exchange 10 ones for a ten. Then add the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_081.jpg |  | Add the 1s. Exchange 10 ones for a ten. Then add the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_082.jpg |
| **Year 2**  **Subtraction** |  |  |  |
| **Subtracting multiples of 10** | Use known number bonds and unitising to subtract multiples of 10.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_083.jpg  *8 subtract 6 is 2.*  *So, 8 tens subtract 6 tens is 2 tens.* | Use known number bonds and unitising to subtract multiples of 10.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_084.jpg  *10 − 3 = 7*  *So, 10 tens subtract 3 tens is 7 tens.* | Use known number bonds and unitising to subtract multiples of 10.  A picture containing text, clipart  Description automatically generated  *7 tens subtract 5 tens is 2 tens.*  *70 − 50 = 20* |
| **Subtracting a single-digit number** | Subtract the 1s. This may be done in or out of a place value grid.  A close-up of some pills  Description automatically generated with low confidence  Shape  Description automatically generated | Subtract the 1s. This may be done in or out of a place value grid.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_088.jpg  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_089.jpg | Subtract the 1s. Understand the link between counting back and subtracting the 1s using known bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_090.jpg  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_091.jpg *9 − 3 = 6*  *39 − 3 = 36* |
| **Subtracting a single-digit number bridging 10** | Bridge 10 by using known bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_092.jpg  *35 − 6*  *I took away 5 counters, then 1 more.* | Bridge 10 by using known bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_093.jpg  *35 − 6*  *First, I will subtract 5, then 1.* | Bridge 10 by using known bonds.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_094.jpg  *24 − 6 = ?*  *24 − 4 − 2 = ?* |
| **Subtracting a single-digit number using exchange** | Exchange 1 ten for 10 ones. This may be done in or out of a place value grid.  Diagram  Description automatically generated | Exchange 1 ten for 10 ones.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_096.jpg | Exchange 1 ten for 10 ones.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_097.jpg  *25 − 7 = 18* |
| **Subtracting a  2-digit number** | Subtract by taking away.    *61 − 18*  *I took away 1 ten and 8 ones.* | Subtract the 10s and the 1s.  This can be represented on a 100 square.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_099.jpg | Subtract the 10s and the 1s.  This can be represented on a number line.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_100.jpg  *64 − 41 = ?*  *64 − 1 = 63*  *63 − 40 = 23*  *64 − 41 = 23*  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_101.jpg  *46 − 20 = 26*  *26 − 5 = 21*  *46 − 25 = 21* |
| **Subtracting a  2-digit number using place value and columns** | Subtract the 1s. Then subtract the 10s. This may be done in or out of a place value grid.  Chart  Description automatically generated  *38 − 16 = 22* | Subtract the 1s. Then subtract the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_103.jpg | Using column subtraction, subtract the 1s. Then subtract the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_104.jpg |
| **Subtracting a  2-digit number with exchange** |  | Exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_105.jpg | Using column subtraction, exchange 1 ten for 10 ones. Then subtract the 1s. Then subtract the 10s.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_106.jpg |
| **Year 2**  **Multiplication** |  |  |  |
| **Equal groups and repeated addition** | Recognise equal groups and write as repeated addition and as multiplication.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_107.jpg  *3 groups of 5 chairs*  *15 chairs altogether* | Recognise equal groups using standard objects such as counters and write as repeated addition and multiplication.  A picture containing clipart  Description automatically generated  *3 groups of 5*  *15 in total* | Use a number line and write as repeated addition and as multiplication.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_109.jpg  *5 + 5 + 5 = 15*  *3 × 5 = 15* |
| **Using arrays to represent multiplication and support understanding** | Understand the relationship between arrays, multiplication and repeated addition.  A picture containing icon  Description automatically generated  *4 groups of 5* | Understand the relationship between arrays, multiplication and repeated addition.  A picture containing icon  Description automatically generated  *4 groups of 5 … 5 groups of 5* | Understand the relationship between arrays, multiplication and repeated addition.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_112.jpg  *5 × 5 = 25* |
| **Understanding commutativity** | Use arrays to visualise commutativity.  A picture containing text, keyboard  Description automatically generated  *I can see 6 groups of 3.*  *I can see 3 groups of 6.* | Form arrays using counters to visualise commutativity. Rotate the array to show that orientation does not change the multiplication.  A picture containing pallette, cosmetic  Description automatically generated  *This is 2 groups of 6 and also 6 groups of 2.* | Use arrays to visualise commutativity.  A picture containing graphical user interface  Description automatically generated  *4 + 4 + 4 + 4 + 4 = 20*  *5 + 5 + 5 + 5 = 20*  *4 × 5 = 20 and 5 × 4 = 20* |
| **Learning ×2, ×5 and ×10 table facts** | Develop an understanding of how to unitise groups of 2, 5 and 10 and learn corresponding times-table facts.  A picture containing text, clipart  Description automatically generated  *3 groups of 10 … 10, 20, 30*  *3 × 10 = 30* | Understand how to relate counting in unitised groups and repeated addition with knowing key times-table facts.  Diagram, rectangle  Description automatically generated  *10 + 10 + 10 = 30*  *3 × 10 = 30* | Understand how the times-tables increase and contain patterns.  A picture containing chat or text message  Description automatically generated  *5 × 10 = 50*  *6 × 10 = 60* |
| **Year 2**  **Division** |  |  |  |
| **Sharing equally** | Start with a whole and share into equal parts, one at a time.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_119.jpg  *12 shared equally between 2.  They get 6 each.*  Start to understand how this also relates to grouping. To share equally between 3 people, take a group of 3 and give 1 to each person. Keep going until all the objects have been shared  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_122.jpg  *15 shared equally between 3.  They get 5 each.* | Represent the objects shared into equal parts using a bar model.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_120.jpg  *20 shared into 5 equal parts.*  *There are 4 in each part.* | Use a bar model to support understanding of the division.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_121.jpg  *18 ÷ 2 = 9* |
| **Grouping equally** | Understand how to make equal groups from a whole.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_123.jpg  *8 divided into 4 equal groups.*  *There are 2 in each group.* | Understand the relationship between grouping and the division statements.  Diagram  Description automatically generated | Understand how to relate division by grouping to repeated subtraction.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_125.jpg  *12 divided into groups of 3.*  *12 ÷ 3 = 4*  *There are 4 groups.* |
| **Using known times-tables to solve divisions** | Understand the relationship between multiplication facts and division.  A group of red cars  Description automatically generated with low confidence  *4 groups of 5 cars is 20 cars in total.*  *20 divided by 4 is 5.* | Link equal grouping with repeated subtraction and known times-table facts to support division.    *40 divided by 4 is 10.*  Use a bar model to support understanding of the link between times-table knowledge and division.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_128.jpg | Relate times-table knowledge directly to division.  C:\Users\Julie\Documents\0_JUST CONTENT\Power maths\Calculator policy\TO DO\artworks\aw_129.jpg  *I know that 3 groups of 10 makes 30, so I know that 30 divided by 10 is 3.*  *3 × 10 = 30 so 30 ÷ 10 = 3* |

**Lower Key Stage 2**

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| LOWER KEY STAGE 2 |
| In Years 3 and 4, children develop the basis of written methods by building their skills alongside a deep understanding of place value. They should use known addition/subtraction and multiplication/division facts to calculate efficiently and accurately, rather than relying on counting. Children use place value equipment to support their understanding, but not as a substitute for thinking. |
| Key language: partition, place value, tens, hundreds, thousands, column method, whole, part, equal groups, sharing, grouping, bar model |

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| PROGRESSION IN CALCULATION IN LOWER KEY STAGE 2 | | |
| Addition and subtraction: In Year 3 especially, the column methods are built up gradually. Children will develop their understanding of how each stage of the calculation, including any exchanges, relates to place value. The example calculations chosen to introduce the stages of each method may often be more suited to a mental method. However, the examples and the progression of the steps have been chosen to help children develop their fluency in the process, alongside a deep understanding of the concepts and the numbers involved, so that they can apply these skills accurately and efficiently to later calculations. The class should be encouraged to compare mental and written methods for specific calculations, and children should be encouraged at every stage to make choices about which methods to apply.  In Year 4, the steps are shown without such fine detail, although children should continue to build their understanding with a secure basis in place value. In subtraction, children will need to develop their understanding of exchange as they may need to exchange across one or two columns.  By the end of Year 4, children should have developed fluency in column methods alongside a deep understanding, which will allow them to progress confidently in upper Key Stage 2. | Multiplication and division: Children build a solid grounding in times-tables, understanding the multiplication and division facts in tandem. As such, they should be as confident knowing that 35 divided by 7 is 5 as knowing that 5 times 7 is 35.  Children develop key skills to support multiplication methods: unitising, commutativity, and how to use partitioning effectively.  Unitising allows children to use known facts to multiply and divide multiples of 10 and 100 efficiently. Commutativity gives children flexibility in applying known facts to calculations and problem solving. An understanding of partitioning allows children to extend their skills to multiplying and dividing 2- and 3-digit numbers by a single digit.  Children develop column methods to support multiplications in these cases.  For successful division, children will need to make choices about how to partition. For example, to divide 423 by 3, it is effective to partition 423 into 300, 120 and 3, as these can be divided by 3 using known facts.  Children will also need to understand the concept of remainder, in terms of a given calculation and in terms of the context of the problem. | Fractions: Children develop the key concept of equivalent fractions, and link this with multiplying and dividing the numerators and denominators, as well as exploring the visual concept through fractions of shapes. Children learn how to find a fraction of an amount, and develop this with the aid of a bar model and other representations alongside.  in Year 3, children develop an understanding of how to add and subtract fractions with the same denominator and find complements to the whole. This is developed alongside an understanding of fractions as numbers, including fractions greater than 1. In Year 4, children begin to work with fractions greater than 1.  Decimals are introduced, as tenths in Year 3 and then as hundredths in Year 4. Children develop an understanding of decimals in terms of the relationship with fractions, with dividing by 10 and 100, and also with place value. |

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| Year 3 | | | |
|  | **Concrete** | **Pictorial** | **Abstract** |
| **Year 3**  **Addition** |  |  |  |
| **Understanding 100s** | Understand the cardinality of 100, and the link with 10 tens.  Use cubes to place into groups of 10 tens.  Background pattern  Description automatically generated | Unitise 100 and count in steps of 100.  A picture containing graphical user interface  Description automatically generated | Represent steps of 100 on a number line and a number track and count up to 1,000 and back to 0.  Diagram  Description automatically generated with medium confidence |
| **Understanding place value to 1,000** | Unitise 100s, 10s and 1s to build 3-digit numbers.  A picture containing text, clipart  Description automatically generated | Use equipment to represent numbers to 1,000.  A picture containing text, clipart  Description automatically generated  Use a place value grid to support the structure of numbers to 1,000.  Place value counters are used alongside other equipment. Children should understand how each counter represents a different unitised amount. | Represent the parts of numbers to 1,000 using a part-whole model.  A picture containing text, clipart  Description automatically generated  *215 = 200 + 10 + 5*  Recognise numbers to 1,000 represented on a number line, including those between intervals. |
| **Adding 100s** | Use known facts and unitising to add multiples of 100.  Diagram  Description automatically generated with medium confidence  *3 + 2 = 5*  *3 hundreds + 2 hundreds = 5 hundreds*  *300 + 200 = 500* | Use known facts and unitising to add multiples of 100.  A picture containing text, clipart  Description automatically generated  *3 + 4 = 7*  *3 hundreds + 4 hundreds = 7 hundreds*  *300 + 400 = 700* | Use known facts and unitising to add multiples of 100.  Represent the addition on a number line.  Use a part-whole model to support unitising.  A picture containing athletic game, sport, basketball  Description automatically generated  *3 + 2 = 5*  *300 + 200 = 500* |
| **3-digit number + 1s, no exchange or bridging** | Use number bonds to add the 1s.  A picture containing diagram  Description automatically generated  *214 + 4 = ?*  *Now there are 4 + 4 ones in total.*  *4 + 4 = 8*  *214 + 4 = 218* | Use number bonds to add the 1s.  Table, calendar  Description automatically generated  *245 + 4*  *5 + 4 = 9*  *245 + 4 = 249* | Understand the link with counting on.  245 + 4  A picture containing timeline  Description automatically generated  Use number bonds to add the 1s and understand that this is more efficient and less prone to error.  *245 + 4 = ?*  *I will add the 1s.*  *5 + 4 = 9*  *So, 245 + 4 = 249* |
| **3-digit number + 1s with exchange** | Understand that when the 1s sum to 10 or more, this requires an exchange of 10 ones for 1 ten.  Children should explore this using unitised objects or physical apparatus. | Exchange 10 ones for 1 ten where needed. Use a place value grid to support the understanding.  A picture containing calendar  Description automatically generated  Diagram  Description automatically generated  Diagram, table  Description automatically generated  135 + 7 = 142 | Understand how to bridge by partitioning to the 1s to make the next 10.  Shape  Description automatically generated  *135 + 7 = ?*  *135 + 5 + 2 = 142*  Ensure that children understand how to add 1s bridging a 100.  *198 + 5 = ?*  *198 + 2 + 3 = 203* |
| **3-digit number + 10s, no exchange** | Calculate mentally by forming the number bond for the 10s.  A picture containing text  Description automatically generated  234 + 50  There are 3 tens and 5 tens altogether.  3 + 5 = 8  In total there are 8 tens.  234 + 50 = 284 | Calculate mentally by forming the number bond for the 10s.  351 + 30 = ?  Diagram  Description automatically generated  *5 tens + 3 tens = 8 tens*  *351 + 30 = 381* | Calculate mentally by forming the number bond for the 10s.  *753 + 40*  *I know that 5 + 4 = 9*  *So, 50 + 40 = 90*  *753 + 40 = 793* |
| **3-digit number + 10s, with exchange** | Understand the exchange of 10 tens for 1 hundred.  A picture containing clipart  Description automatically generated | Add by exchanging 10 tens for 1 hundred.  184 + 20 = ?  Diagram  Description automatically generated  *184 + 20 = 204* | Understand how the addition relates to counting on in 10s across 100.  A picture containing sport  Description automatically generated  *184 + 20 = ?*  *I can count in 10s … 194 … 204*  *184 + 20 = 204*  Use number bonds within 20 to support efficient mental calculations.  *385 + 50*  *There are 8 tens and 5 tens.*  *That is 13 tens.*  *385 + 50 = 300 + 130 + 5*  *385 + 50 = 435* |
| **3-digit number + 2-digit number** | Use place value equipment to make and combine groups to model addition. | Use a place value grid to organise thinking and adding of 1s, then 10s. | Use the vertical column method to represent the addition. Children must understand how this relates to place value at each stage of the calculation. |
| **3-digit number + 2-digit number, exchange required** | Use place value equipment to model addition and understand where exchange is required.  *Use place value counters to represent*  *154 + 72.*  *Use this to decide if any exchange is required.*  *There are 5 tens and 7 tens. That is 12 tens so I will exchange.* | Represent the required exchange on a place value grid using equipment.  *275 + 16 = ?*  Diagram  Description automatically generated  *275 + 16 = 291*  Note: In this example, a mental method may be more efficient. The numbers for the example calculation have been chosen to allow children to visualise the concept and see how the method relates to place value.  Children should be encouraged at every stage to select methods that are accurate and efficient. | Use a column method with exchange. Children must understand how the method relates to place value at each stage of the calculation.  A screenshot of a phone  Description automatically generated with low confidence  *275 + 16 = 291* |
| **3-digit number + 3-digit number, no exchange** | Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.  326 + 541 is represented as:  Calendar  Description automatically generated | Represent the place value grid with equipment to model the stages of column addition. | Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation. |
| **3-digit number + 3-digit number, exchange required** | Use place value equipment to enact the exchange required.  Diagram  Description automatically generated  *There are 13 ones.*  *I will exchange 10 ones for 1 ten.* | Model the stages of column addition using place value equipment on a place value grid. | Use column addition, ensuring understanding of place value at every stage of the calculation.  A screenshot of a phone  Description automatically generated with low confidence  *126 + 217 = 343*  Note: Children should also study examples where exchange is required in more than one column, for example *185 + 318 = ?* |
| **Representing addition problems, and selecting appropriate methods** | Encourage children to use their own drawings and choices of place value equipment to represent problems with one or more steps.  These representations will help them to select appropriate methods. | Children understand and create bar models to represent addition problems.  *275 + 99 = ?*  Table  Description automatically generated with medium confidence  *275 + 99 = 374* | Use representations to support choices of appropriate methods.  A picture containing diagram  Description automatically generated  *I will add 100, then subtract 1 to find the solution.*  *128 + 105 + 83 = ?*  *I need to add three numbers.*  A picture containing diagram  Description automatically generated |
| **Year 3**  **Subtraction** |  |  |  |
| **Subtracting 100s** | Use known facts and unitising to subtract multiples of 100.  Diagram, table  Description automatically generated  *5 − 2 = 3*  *500 − 200 = 300* | Use known facts and unitising to subtract multiples of 100.  A picture containing text, building  Description automatically generated  *4 − 2 = 2*  *400 − 200 = 200* | Understand the link with counting back in 100s.  A picture containing text, clipart  Description automatically generated  *400 − 200 = 200*  Use known facts and unitising as efficient and accurate methods.  I know that 7 − 4 = 3. Therefore, I know that 700 − 400 = 300. |
| **3-digit number − 1s, no exchange** | Use number bonds to subtract the 1s.  Company name  Description automatically generated  *214 − 3 = ?*  Logo, company name  Description automatically generated  *4 − 3 = 1*  *214 − 3 = 211* | Use number bonds to subtract the 1s.  Diagram  Description automatically generated with low confidence  *319 − 4 = ?*  Diagram  Description automatically generated  *9 − 4 = 5*  *319 − 4 = 315* | Understand the link with counting back using a number line.  Use known number bonds to calculate mentally.  476 − 4 = ?  A picture containing text, clipart  Description automatically generated  6 − 4 = 2  476 − 4 = 472 |
| **3-digit number − 1s, exchange or bridging required** | Understand why an exchange is necessary by exploring why 1 ten must be exchanged.  Use place value equipment. | Represent the required exchange on a place value grid.  151 − 6 = ?  Diagram  Description automatically generated | Calculate mentally by using known bonds.  151 − 6 = ?  151 − 1 − 5 = 145 |
| **3-digit number − 10s, no exchange** | Subtract the 10s using known bonds.  Chart  Description automatically generated with medium confidence  *381 − 10 = ?*  *8 tens with 1 removed is 7 tens.*  *381 − 10 = 371* | Subtract the 10s using known bonds.  Diagram, table  Description automatically generated  *8 tens − 1 ten = 7 tens*  *381 − 10 = 371* | Use known bonds to subtract the 10s mentally.  *372 − 50 = ?*  *70 − 50 = 20*  *So, 372 − 50 = 322* |
| **3-digit number − 10s, exchange or bridging required** | Use equipment to understand the exchange of 1 hundred for 10 tens.  A picture containing text, clipart  Description automatically generated | Represent the exchange on a place value grid using equipment.  210 − 20 = ?  Diagram  Description automatically generated  I need to exchange 1 hundred for 10 tens, to help subtract 2 tens.  Diagram, table  Description automatically generated  *210 − 20 = 190* | Understand the link with counting back on a number line.  Use flexible partitioning to support the calculation.  235 − 60 = ?  A picture containing text, clipart  Description automatically generated  235 = 100 + 130 + 5  235 − 60 = 100 + 70 + 5  = 175 |
| **3-digit number − up to 3-digit number** | Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.  A picture containing chart  Description automatically generated | Represent the calculation on a place value grid.  Chart  Description automatically generated | Use column subtraction to calculate accurately and efficiently.  A picture containing text, clock  Description automatically generated |
| **3-digit number − up to 3-digit number, exchange required** | Use equipment to enact the exchange of 1 hundred for 10 tens, and 1 ten for 10 ones.  Diagram  Description automatically generated | Model the required exchange on a place value grid.  175 − 38 = ?  *I need to subtract 8 ones, so I will exchange a ten for 10 ones.*  Diagram, table  Description automatically generated  Diagram  Description automatically generated | Use column subtraction to work accurately and efficiently.  A picture containing text, clock  Description automatically generated  If the subtraction is a 3-digit number subtract a 2-digit number, children should understand how the recording relates to the place value, and so how to line up the digits correctly.  Children should also understand how to exchange in calculations where there is a zero in the 10s column.  A picture containing calendar  Description automatically generated |
| **Representing subtraction problems** |  | Use bar models to represent subtractions.  ‘Find the difference’ is represented as two bars for comparison.  Diagram  Description automatically generated  Bar models can also be used to show that a part must be taken away from the whole. | Children use alternative representations to check calculations and choose efficient methods.  Children use inverse operations to check additions and subtractions.  The part-whole model supports understanding.  I have completed this subtraction.  525 − 270 = 255  I will check using addition.  A picture containing text, clipart  Description automatically generated |
| **Year 3**  **Multiplication** |  |  |  |
| **Understanding equal grouping and repeated addition** | Children continue to build understanding of equal groups and the relationship with repeated addition.  They recognise both examples and non-examples using objects.  A picture containing clipart, vector graphics  Description automatically generated  Children recognise that arrays can be used to model commutative multiplications.  A picture containing text, furniture, fabric  Description automatically generated  I can see 3 groups of 8.  I can see 8 groups of 3. | Children recognise that arrays demonstrate commutativity.  A picture containing text, clipart  Description automatically generated  *This is 3 groups of 4.*  *This is 4 groups of 3.* | Children understand the link between repeated addition and multiplication.  Diagram  Description automatically generated  8 groups of 3 is 24.  3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24  8 × 3 = 24  A bar model may represent multiplications as equal groups.  Diagram  Description automatically generated  *6 × 4 = 24* |
| **Using commutativity to support understanding of the times-tables** | Understand how to use times-tables facts flexibly.  A group of toothbrushes  Description automatically generated with medium confidence  Chart, bubble chart  Description automatically generated  *There are 6 groups of 4 pens.*  *There are 4 groups of 6 bread rolls.*  *I can use 6 × 4 = 24 to work out both totals.* | Understand how times-table facts relate to commutativity.  A group of red circles  Description automatically generated with low confidence  6 × 4 = 24  4 × 6 = 24 | Understand how times-table facts relate to commutativity.  *I need to work out 4 groups of 7.*  *I know that 7 × 4 = 28*  *so, I know that*  *4 groups of 7 = 28*  *and*  *7 groups of 4 = 28.* |
| **Understanding and using ×3, ×2, ×4 and ×8 tables.** | Children learn the times-tables as ‘groups of’, but apply their knowledge of commutativity.      *I can use the ×3 table to work out how many keys.*  *I can also use the ×3 table to work out how many batteries.* | Children understand how the ×2, ×4 and ×8 tables are related through repeated doubling.  A picture containing calculator, remote control, clipart, vector graphics  Description automatically generated | Children understand the relationship between related multiplication and division facts in known times-tables.  A picture containing text, clipart  Description automatically generated  *2 × 5 = 10*  *5 × 2 = 10*  *10 ÷ 5 = 2*  *10 ÷ 2 = 5* |
| **Using known facts to multiply 10s, for example 3 × 40** | Explore the relationship between known times-tables and multiples of 10 using place value equipment.  *Make 4 groups of 3 ones.*    *Make 4 groups of 3 tens.*  A picture containing text, clipart  Description automatically generated  *What is the same?*  *What is different?* | Understand how unitising 10s supports multiplying by multiples of 10.  Shape  Description automatically generated  A picture containing text, clipart, keyboard  Description automatically generated  *4 groups of 2 ones is 8 ones.*  *4 groups of 2 tens is 8 tens.*  *4 × 2 = 8*  *4 × 20 = 80* | Understand how to use known times-tables to multiply multiples of 10.  A picture containing text, clock  Description automatically generated  A picture containing diagram  Description automatically generated  4 × 2 = 8  4 × 20 = 80 |
| **Multiplying a  2-digit number by a 1-digit number** | Understand how to link partitioning a 2-digit number with multiplying.  Each person has 23 flowers.  Each person has 2 tens and 3 ones.  A picture containing clipart, doll  Description automatically generated  There are 3 groups of 2 tens.  There are 3 groups of 3 ones.  Use place value equipment to model the multiplication context.  Diagram, table  Description automatically generated  There are 3 groups of 3 ones.  There are 3 groups of 2 tens. | Use place value to support how partitioning is linked with multiplying by a 2-digit number.  3 × 24 = ?  Diagram  Description automatically generated  3 × 4 = 12  Diagram, table  Description automatically generated  3 × 20 = 60  60 + 12 = 72  3 × 24 = 72 | Use addition to complete multiplications of 2-digit numbers by a 1-digit number.  4 × 13 = ?  4 × 3 = 12 4 × 10 = 40  12 + 40 = 52  4 × 13 = 52 |
| **Multiplying a  2-digit number by a 1-digit number, expanded column method** | Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications.  *3 × 24 = ?*  *3 × 20 = 60*  *3 × 4 = 12*  A screenshot of a computer  Description automatically generated with medium confidence  *3 × 24 = 60 + 12*  *3 × 24 = 70 + 2*  *3 × 24 = 72* | Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s.  *4 × 23 = ?*  Diagram  Description automatically generated  *4 × 23 = 92*  Diagram  Description automatically generated  *5 × 23 = ?*  *5 × 3 = 15*  *5 × 20 = 100*  *5 × 23 = 115* | Children may write calculations in expanded column form, but must understand the link with place value and exchange.  Children are encouraged to write the expanded parts of the calculation separately.  Diagram  Description automatically generated  5 × 28 = ?  A picture containing text, clock  Description automatically generated |
| **Year 3**  **Division** |  |  |  |
| **Using times-tables knowledge to divide** | Use knowledge of known times-tables to calculate divisions.  Icon  Description automatically generated with medium confidence  24 divided into groups of 8.  There are 3 groups of 8. | Use knowledge of known times-tables to calculate divisions.  A picture containing text, fabric  Description automatically generated  48 divided into groups of 4.  There are 12 groups.  4 × 12 = 48  48 ÷ 4 = 12 | Use knowledge of known times-tables to calculate divisions.  *I need to work out 30 shared between 5.*  *I know that 6 × 5 = 30  so I know that 30 ÷ 5 = 6.*  A bar model may represent the relationship between sharing and grouping.  Diagram  Description automatically generated  *24 ÷ 4 = 6*  *24 ÷ 6 = 4*  Children understand how division is related to both repeated subtraction and repeated addition.  Diagram  Description automatically generated  *24 ÷ 8 = 3*  A picture containing timeline  Description automatically generated  *32 ÷ 8 = 4* |
| **Understanding remainders** | Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.    *There are 13 sticks in total.*  *There are 3 groups of 4, with 1 remainder.* | Use images to explain remainders.  A group of red circles  Description automatically generated with medium confidence  *22 ÷ 5 = 4 remainder 2* | Understand that the remainder is what cannot be shared equally from a set.  *22 ÷ 5 = ?*  *3 × 5 = 15*  *4 × 5 = 20*  *5 × 5 = 25 … this is larger than 22*  *So, 22 ÷ 5 = 4 remainder 2* |
| **Using known facts to divide multiples of 10** | Use place value equipment to understand how to divide by unitising.  Make 6 ones divided by 3.  Diagram  Description automatically generated with medium confidence  Now make 6 tens divided by 3.  A picture containing text, clipart  Description automatically generated  What is the same? What is different? | Divide multiples of 10 by unitising.  A picture containing text, clipart  Description automatically generated  12 tens shared into 3 equal groups.  4 tens in each group. | Divide multiples of 10 by a single digit using known times-tables.  180 ÷ 3 = ?  180 is 18 tens.  18 divided by 3 is 6.  18 tens divided by 3 is 6 tens.  18 ÷ 3 = 6  180 ÷ 3 = 60 |
| **2-digit number divided by  1-digit number, no remainders** | Children explore dividing 2-digit numbers by using place value equipment.  A picture containing text, clipart  Description automatically generated  48 ÷ 2 = ?  First divide the 10s.  A picture containing chat or text message  Description automatically generated  Then divide the 1s.  Icon  Description automatically generated | Children explore which partitions support particular divisions.  A picture containing text, clipart  Description automatically generated  *I need to partition 42 differently to divide by 3.*  A picture containing text, clipart  Description automatically generated  *42 = 30 + 12*  *42 ÷ 3 = 14* | Children partition a number into 10s and 1s to divide where appropriate.  Circle  Description automatically generated with medium confidence  *60 ÷ 2 = 30*  *8 ÷ 2 = 4*  *30 + 4 = 34*  *68 ÷ 2 = 34*  Children partition flexibly to divide where appropriate.  42 ÷ 3 = ?  42 = 40 + 2  *I need to partition 42 differently to divide*  *by 3.*  *42 = 30 + 12*  *30 ÷ 3 = 10*  *12 ÷ 3 = 4*  *10 + 4 = 14*  *42 ÷ 3 = 14* |
| **2-digit number divided by  1-digit number, with remainders** | Use place value equipment to understand the concept of remainder.  *Make 29 from place value equipment.*  *Share it into 2 equal groups*.  A picture containing text, clipart, screenshot  Description automatically generated  *There are two groups of 14 and*  *1 remainder.* | Use place value equipment to understand the concept of remainder in division.  *29 ÷ 2 = ?*  A picture containing text, clipart  Description automatically generated  *29 ÷ 2 = 14 remainder 1* | Partition to divide, understanding the remainder in context.  *67 children try to make 5 equal lines.*  *67 = 50 + 17*  *50 ÷ 5 = 10*  *17 ÷ 5 = 3 remainder 2*  *67 ÷ 5 = 13 remainder 2*  *There are 13 children in each line and*  *2 children left out.* |
| Year 4 | | | |
|  | **Concrete** | **Pictorial** | **Abstract** |
| **Year 4**  **Addition** |  |  |  |
| **Understanding numbers to 10,000** | Use place value equipment to understand the place value of 4-digit numbers.  A picture containing shape  Description automatically generated  4 thousands equal 4,000.  1 thousand is 10 hundreds. | Represent numbers using place value counters once children understand the relationship between 1,000s and 100s.    2,000 + 500 + 40 + 2 = 2,542 | Understand partitioning of 4-digit numbers, including numbers with digits of 0.  Diagram  Description automatically generated  5,000 + 60 + 8 = 5,068  Understand and read 4-digit numbers on a number line.  A picture containing antenna  Description automatically generated |
| **Choosing mental methods where appropriate** | Use unitising and known facts to support mental calculations.  *Make 1,405 from place value equipment.*  *Add 2,000.*  *Now add the 1,000s.*  *1 thousand + 2 thousands = 3 thousands*  *1,405 + 2,000 = 3,405* | Use unitising and known facts to support mental calculations.  Chart  Description automatically generated with low confidence  *I can add the 100s mentally.*  *200 + 300 = 500*  *So, 4,256 + 300 = 4,556* | Use unitising and known facts to support mental calculations.  *4,256 + 300 = ?*  *2 + 3 = 5 200 + 300 = 500*  *4,256 + 300 = 4,556* |
| **Column addition with exchange** | Use place value equipment on a place value grid to organise thinking.  Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers.  *Use equipment.to show 1,905 + 775.*  Chart  Description automatically generated with low confidence  *Why have only three columns been used for the second row? Why is the Thousands box empty?*  *Which columns will total 10 or more?* | Use place value equipment to model required exchanges.  Calendar  Description automatically generated  Include examples that exchange in more than one column. | Use a column method to add, including exchanges.  A picture containing text, clock  Description automatically generated  Include examples that exchange in more than one column. |
| **Representing additions and checking strategies** |  | Bar models may be used to represent additions in problem contexts, and to justify mental methods where appropriate.  A picture containing diagram  Description automatically generated  *I chose to work out 574 + 800,  then subtract 1.*  Chart, box and whisker chart  Description automatically generated  *This is equivalent to 3,000 + 3,000.* | Use rounding and estimating on a number line to check the reasonableness of an addition.    *912 + 6,149 = ?*  *I used rounding to work out that the  answer should be approximately  1,000 + 6,000 = 7,000.* |
| **Year 4**  **Subtraction** |  |  |  |
| **Choosing mental methods where appropriate** | Use place value equipment to justify mental methods.  Shape  Description automatically generated  *What number will be left if we take away 300?* | Use place value grids to support mental methods where appropriate.  A picture containing diagram  Description automatically generated  *7,646 − 40 = 7,606* | Use knowledge of place value and unitising to subtract mentally where appropriate.  3,501 − 2,000  3 thousands − 2 thousands = 1 thousand  3,501 − 2,000 = 1,501 |
| **Column subtraction with exchange** | Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.  A picture containing diagram  Description automatically generated | Represent place value equipment on a place value grid to subtract, including exchanges where needed.  Calendar  Description automatically generated with medium confidence | Use column subtraction, with understanding of the place value of any exchange required.  A picture containing text, clock  Description automatically generated |
| **Column subtraction with exchange across more than one column** | Understand why two exchanges may be necessary.  *2,502 − 243 = ?*  A picture containing cage  Description automatically generated  *I need to exchange a 10 for some 1s, but there are not any 10s here.*  Diagram  Description automatically generated | Make exchanges across more than one column where there is a zero as a place holder.  *2,502 − 243 = ?*  A screenshot of a game  Description automatically generated with medium confidence  A screenshot of a game  Description automatically generated with low confidence | Make exchanges across more than one column where there is a zero as a place holder.  *2,502 − 243 = ?*  A picture containing object  Description automatically generated |
| **Representing subtractions and checking strategies** |  | Use bar models to represent subtractions where a part needs to be calculated.  Table  Description automatically generated  *I can work out the total number of Yes votes using 5,762 − 2,899.*  Bar models can also represent ‘find the difference’ as a subtraction problem.  Table  Description automatically generated | Use inverse operations to check subtractions.  *I calculated 1,225 − 799 = 574.*  *I will check by adding the parts.*  Diagram  Description automatically generated with medium confidence  *The parts do not add to make 1,225.*  *I must have made a mistake.* |
| **Year 4**  **Multiplication** |  |  |  |
| **Multiplying by multiples of 10 and 100** | Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.  A picture containing text, shoji, building  Description automatically generated  *3 groups of 4 ones is 12 ones.*  *3 groups of 4 tens is 12 tens.*  *3 groups of 4 hundreds is 12 hundreds.* | Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.  A picture containing text, shoji, building  Description automatically generated  *3 × 4 = 12*  *3 × 40 = 120*  *3 × 400 = 1,200* | Use known facts and understanding of place value and commutativity to multiply mentally.  *4 × 7 = 28*  *4 × 70 = 280*  *40 × 7 = 280*  *4 × 700 = 2,800*  *400 × 7 = 2,800* |
| **Understanding times-tables up to 12 × 12** | Understand the special cases of multiplying by 1 and 0.  A picture containing table, basket, bowl, container  Description automatically generated  5 × 1 = 5 5 × 0 = 0 | Represent the relationship between the ×9 table and the ×10 table.  A picture containing table  Description automatically generated  Represent the ×11 table and ×12 tables in relation to the ×10 table.  A picture containing text  Description automatically generated  2 × 11 = 20 + 2  3 × 11 = 30 + 3  4 × 11 = 40 + 4  A picture containing text, clipart  Description automatically generated  4 × 12 = 40 + 8 | Understand how times-tables relate to counting patterns.  Understand links between the  ×3 table, ×6 table and ×9 table  *5* × *6 is double 5* × *3*  ×5 table and ×6 table  *I know that 7* × *5 = 35  so I know that 7 × 6 = 35 + 7.*  ×5 table and ×7 table  *3 × 7 = 3 × 5 + 3 × 2*  Chart, diagram  Description automatically generated  ×9 table and ×10 table  *6 × 10 = 60*  *6 × 9 = 60 − 6* |
| **Understanding and using partitioning in multiplication** | Make multiplications by partitioning.  *4 × 12 is 4 groups of 10 and 4 groups of 2.*  A picture containing text, clipart  Description automatically generated  *4 × 12 = 40 + 8* | Understand how multiplication and partitioning are related through addition.  Diagram  Description automatically generated with low confidence  *4 × 3 = 12*  *4 × 5 = 20*  *12 + 20 = 32*  *4 × 8 = 32* | Use partitioning to multiply 2-digit numbers by a single digit.  18 × 6 = ?  A picture containing text, clipart  Description automatically generated  18 × 6 = 10 × 6 + 8 × 6  = 60 + 48  = 108 |
| **Column multiplication for 2- and  3-digit numbers multiplied by a single digit** | Use place value equipment to make multiplications.  Make 4 × 136 using equipment.  A picture containing clipart  Description automatically generated  *I can work out how many 1s, 10s and 100s.*  *There are 4 × 6 ones… 24 ones*  *There are 4 × 3 tens … 12 tens*  *There are 4 × 1 hundreds … 4 hundreds*  *24 + 120 + 400 = 544* | Use place value equipment alongside a column method for multiplication of up to  3-digit numbers by a single digit.  A picture containing text, clipart  Description automatically generated | Use the formal column method for up to  3-digit numbers multiplied by a single digit.  A picture containing text, clock  Description automatically generated  Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation.  A picture containing text, clock  Description automatically generated |
| **Multiplying more than two numbers** | Represent situations by multiplying three numbers together.  *A picture containing text  Description automatically generated*  *Each sheet has 2 × 5 stickers.*  *There are 3 sheets*.  *There are 5 × 2 × 3 stickers in total.*  Diagram, text  Description automatically generated with medium confidence | Understand that commutativity can be used to multiply in different orders.  Shape, circle  Description automatically generated  2 × 6 × 10 = 120  12 × 10 = 120  10 × 6 × 2 = 120  60 × 2 = 120 | Use knowledge of factors to simplify some multiplications.  24 × 5 = 12 × 2 × 5  Diagram, schematic  Description automatically generated |
| **Year 4**  **Division** |  |  |  |
| **Understanding the relationship between multiplication and division, including times-tables** | Use objects to explore families of multiplication and division facts.  Shape, circle  Description automatically generated  *4 × 6 = 24*  *24 is 6 groups of 4.*  *24 is 4 groups of 6.*  *24 divided by 6 is 4.*  *24 divided by 4 is 6*. | Represent divisions using an array.    Bubble chart  Description automatically generated with medium confidence | Understand families of related multiplication and division facts.  I know that 5 × 7 = 35  so I know all these facts:  5 × 7 = 35  7 × 5 = 35  35 = 5 × 7  35 = 7 × 5  35 ÷ 5 = 7  35 ÷ 7 = 5  7 = 35 ÷ 5  5 = 35 ÷ 7 |
| **Dividing multiples of 10 and 100 by a single digit** | Use place value equipment to understand how to use unitising to divide.  Calendar  Description automatically generated with medium confidence  *8 ones divided into 2 equal groups*  *4 ones in each group*  *8 tens divided into 2 equal groups*  *4 tens in each group*  *8 hundreds divided into 2 equal groups*  *4 hundreds in each group* | Represent divisions using place value equipment.  A screenshot of a cell phone  Description automatically generated with low confidence  *9 ÷ 3 = 3*  *9 tens divided by 3 is 3 tens.*  *9 hundreds divided by 3 is 3 hundreds.* | Use known facts to divide 10s and 100s by a single digit.  15 ÷ 3 = 5  150 ÷ 3 = 50  1500 ÷ 3 = 500 |
| **Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s** | Partition into 10s and 1s to divide where appropriate.  *39 ÷ 3 = ?*  Diagram, box and whisker chart  Description automatically generated  *39 = 30 + 9*  *30 ÷ 3 = 10*  *9 ÷ 3 = 3*  *39 ÷ 3 = 13* | Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate.  *39 ÷ 3 = ?*  A picture containing text, clipart  Description automatically generated  *39 = 30 + 9*  *30 ÷ 3 = 10*  *9 ÷ 3 = 3*  *39 ÷ 3 = 13* | Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate.  142 ÷ 2 = ?  A picture containing text, clipart  Description automatically generated  100 ÷ 2 = 50  40 ÷ 2 = 20  6 ÷ 2 = 3  50 + 20 + 3 = 73  142 ÷ 2 = 73 |
| **Dividing 2-digit and 3-digit numbers by a single digit, using flexible partitioning** | Use place value equipment to explore why different partitions are needed.  42 ÷ 3 = ?  *I will split it into 30 and 12, so that I can divide by 3 more easily.*  A picture containing clipart  Description automatically generated | Represent how to partition flexibly where needed.  84 ÷ 7 = ?  I will partition into 70 and 14 because I am dividing by 7.  Background pattern  Description automatically generated with medium confidence | Make decisions about appropriate partitioning based on the division required.  A picture containing text, clipart  Description automatically generated  Understand that different partitions can be used to complete the same division.  Diagram, shape  Description automatically generated |
| **Understanding remainders** | Use place value equipment to find remainders.  85 shared into 4 equal groups  There are 24, and 1 that cannot be shared.  A picture containing text, clipart  Description automatically generated | Represent the remainder as the part that cannot be shared equally.    72 ÷ 5 = 14 remainder 2 | Understand how partitioning can reveal remainders of divisions.  A picture containing text, clipart  Description automatically generated  80 ÷ 4 = 20  12 ÷ 4 = 3  95 ÷ 4 = 23 remainder 3 |

**UPPER KEY STAGE 2**

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| UPPER KEY STAGE 2 | | |
| In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations. | | |
| Key language: decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number | | |
| Progression in calculation in Upper Key Stage 2 | | |
| Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.  Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.  Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen. | Multiplication and division: Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.  Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.  Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.  Multiplication and division of decimals are also introduced and refined in Year 6. | Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them.  Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.  Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%. |

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| Year 5 | | | |
|  | **Concrete** | **Pictorial** | **Abstract** |
| **Year 5**  **Addition** |  |  |  |
| **Column addition with whole numbers** | Use place value equipment to represent additions.  Add a row of counters onto the place value grid to show 15,735 + 4,012.  Diagram  Description automatically generated with medium confidence | Represent additions, using place value equipment on a place value grid alongside written methods.  Chart  Description automatically generated  *I need to exchange 10 tens for a 100.*  Table  Description automatically generated with low confidence | Use column addition, including exchanges.  A picture containing calendar  Description automatically generated |
| **Representing additions** |  | Bar models represent addition of two or more numbers in the context of problem solving.  Timeline  Description automatically generated with low confidence  Diagram  Description automatically generated | Use approximation to check whether answers are reasonable.  A picture containing text, clock  Description automatically generated  *I will use 23,000 + 8,000 to check.* |
| **Adding tenths** | Link measure with addition of decimals.  Two lengths of fencing are 0·6 m and  0·2 m.  How long are they when added together?  Diagram  Description automatically generated | Use a bar model with a number line to add tenths.    0·6 + 0·2 = 0·8  6 tenths + 2 tenths = 8 tenths | Understand the link with adding fractions.  *6 tenths + 2 tenths = 8 tenths*  *0*·*6 + 0*·*2 = 0*·*8* |
| **Adding decimals using column addition** | Use place value equipment to represent additions.  Show 0·23 + 0·45 using place value counters. | Use place value equipment on a place value grid to represent additions.  Represent exchange where necessary.  Chart  Description automatically generated  Include examples where the numbers of decimal places are different.  Table  Description automatically generated | Add using a column method, ensuring that children understand the link with place value.  Table  Description automatically generated  Include exchange where required, alongside an understanding of place value.  A picture containing table  Description automatically generated  Include additions where the numbers of decimal places are different.  3.4 + 0.65 = ?  Table  Description automatically generated with low confidence |
| **Year 5**  **Subtraction** |  |  |  |
| **Column subtraction with whole numbers** | Use place value equipment to understand where exchanges are required.  *2,250 – 1,070*  Chart, bar chart  Description automatically generated with medium confidence | Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.  *15,735 − 2,582 = 13,153*  Timeline  Description automatically generated with low confidence | Use column subtraction methods with exchange where required.  A picture containing text, time  Description automatically generated  62,097 − 18,534 = 43,563 |
| **Checking strategies and representing subtractions** |  | Bar models represent subtractions in problem contexts, including ‘find the difference’.  Diagram  Description automatically generated | Children can explain the mistake made when the columns have not been ordered correctly.  A picture containing text  Description automatically generated  Use approximation to check calculations.  *I calculated 18,000 + 4,000 mentally to check my subtraction.* |
| **Choosing efficient methods** |  |  | To subtract two large numbers that are close, children find the difference by counting on.  2,002 − 1,995 = ?  Diagram  Description automatically generated  Use addition to check subtractions.  *I calculated 7,546 − 2,355 = 5,191.*  *I will check using the inverse.* |
| **Subtracting decimals** | Explore complements to a whole number by working in the context of length.  Diagram  Description automatically generated with low confidence  1 − 0·49 = ? | Use a place value grid to represent the stages of column subtraction, including exchanges where required.  5·74 − 2·25 = ? | Use column subtraction, with an understanding of place value, including subtracting numbers with different numbers of decimal places.  3·921 − 3·75 = ? |
| **Year 5**  **Multiplication** |  |  |  |
| **Understanding factors** | Use cubes or counters to explore the meaning of ‘square numbers’.  *25 is a square number because it is made from 5 rows of 5.*  Use cubes to explore cube numbers.  Diagram  Description automatically generated  8 is a cube number. | Use images to explore examples and non-examples of square numbers.  A black and white checkered surface  Description automatically generated with medium confidence  *8 × 8 = 64*  *82 = 64*  Chart, histogram  Description automatically generated  *12 is not a square number, because you cannot multiply a whole number by itself to make 12.* | Understand the pattern of square numbers in the multiplication tables.  Use a multiplication grid to circle each square number. Can children spot a pattern? |
| **Multiplying by 10, 100 and 1,000** | Use place value equipment to multiply by 10, 100 and 1,000 by unitising.  A picture containing calendar  Description automatically generated | Understand the effect of repeated multiplication by 10.  A picture containing text  Description automatically generated | Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.  Diagram  Description automatically generated  17 × 10 = 170  17 × 100 = 17 × 10 × 10 = 1,700  17 × 1,000 = 17 × 10 × 10 × 10 = 17,000 |
| **Multiplying by multiples of 10, 100 and 1,000** | Use place value equipment to explore multiplying by unitising.  A picture containing text, clipart  Description automatically generated  *5 groups of 3 ones is 15 ones.*  *5 groups of 3 tens is 15 tens.*  *So, I know that 5 groups of 3 thousands would be 15 thousands.* | Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.  A picture containing cosmetic  Description automatically generated  *4 × 3 = 12 6 × 4 = 24*  *4 × 300 = 1,200 6 × 400 = 2,400* | Use known facts and unitising to multiply.  5 × 4 = 20  5 × 40 = 200  5 × 400 = 2,000  5 × 4,000 − 20,000  5,000 × 4 = 20,000 |
| **Multiplying up to 4-digit numbers by a single digit** | Explore how to use partitioning to multiply efficiently.  *8 × 17 = ?*  A picture containing text, calculator  Description automatically generated    *So, 8 × 17 = 136* | Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.  Chart  Description automatically generated | Use an area model and then add the parts.    Text  Description automatically generated with low confidence  Use a column multiplication, including any required exchanges.  A picture containing text, clock  Description automatically generated |
| **Multiplying 2-digit numbers by 2-digit numbers** | Partition one number into 10s and 1s, then add the parts.  *23 × 15 = ?*  Table  Description automatically generated  *23 × 15 = 345* | Use an area model and add the parts.  *28 × 15 = ?*  Table  Description automatically generated  *28 × 15 = 420* | Use column multiplication, ensuring understanding of place value at each stage.  Table  Description automatically generated with medium confidence  Table  Description automatically generated  Table  Description automatically generated |
| **Multiplying up to 4-digits by 2-digits** |  | Use the area model then add the parts.  Table  Description automatically generated with medium confidence  *143 × 12 = 1,716* | Use column multiplication, ensuring understanding of place value at each stage.  A picture containing text, clock  Description automatically generated  Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.  *1,274 × 32 = ?*  *First multiply 1,274 by 2.*  A picture containing text, clock  Description automatically generated  *Then multiply 1,274 by 30.*  A picture containing text, clock  Description automatically generated  *Finally, find the total.*  A picture containing text, clock  Description automatically generated  *1,274 × 32 = 40,768* |
| **Multiplying decimals by 10, 100 and 1,000** | Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths. | Represent multiplication by 10 as exchange on a place value grid.  A picture containing text, calculator  Description automatically generated  0·14 × 10 = 1·4 | Understand how this exchange is represented on a place value chart.  A picture containing table  Description automatically generated |
| **Year 5**  **Division** |  |  |  |
| **Understanding factors and prime numbers** | Use equipment to explore the factors of a given number.  A picture containing cosmetic, toiletry  Description automatically generated  *24 ÷ 3 = 8*  *24 ÷ 8 = 3*  *8 and 3 are factors of 24 because they divide 24 exactly.*  Chart  Description automatically generated  5 is not a factor of 24 because there is a remainder. | Understand that prime numbers are numbers with exactly two factors.  13 ÷ 1 = 13  13 ÷ 2 = 6 r 1  13 ÷ 4 = 4 r 1  *1 and 13 are the only factors of 13.*  *13 is a prime number.* | Understand how to recognise prime and composite numbers.  *I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.*  *I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.*  *I know that 1 is not a prime number, as it has only 1 factor.* |
| **Understanding inverse operations and the link with multiplication, grouping and sharing** | Use equipment to group and share and to explore the calculations that are present.  *I have 28 counters.*  *I made 7 groups of 4. There are 28 in total.*  *I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.*  *I have 28 in total. I made groups of 4. There are 7 equal groups.* | Represent multiplicative relationships and explore the families of division facts.  A picture containing text, calculator, clipart  Description automatically generated  *60 ÷ 4 = 15*  *60 ÷ 15 = 4* | Represent the different multiplicative relationships to solve problems requiring inverse operations.  Diagram  Description automatically generated with medium confidence  Understand missing number problems for division calculations and know how to solve them using inverse operations.  22 ÷ ? = 2  22 ÷ 2 = ?  ? ÷ 2 = 22  ? ÷ 22 = 2 |
| **Dividing whole numbers by 10, 100 and 1,000** | Use place value equipment to support unitising for division.  *4,000 ÷ 1,000*    *4,000 is 4 thousands.*  *4 × 1,000= 4,000*  *So, 4,000 ÷ 1,000 = 4* | Use a bar model to support dividing by unitising.  *380 ÷ 10 = 38*  A screenshot of a computer  Description automatically generated with low confidence  A picture containing line chart  Description automatically generated  *380 is 38 tens.*  *38 × 10 = 380*  *10 × 38 = 380*  *So, 380 ÷ 10 = 38* | Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.  Diagram  Description automatically generated with medium confidence  3,200 ÷ 100 = ?  *3,200 is 3 thousands and 2 hundreds.*  *200 ÷ 100 = 2*  *3,000 ÷ 100 = 30*  *3,200 ÷ 100 = 32*  *So, the digits will move two places to the right.* |
| **Dividing by multiples of 10, 100 and 1,000** | Use place value equipment to represent known facts and unitising.  A picture containing text, clipart  Description automatically generated  *15 ones put into groups of 3 ones. There are 5 groups.*  *15 ÷ 3 = 5*  *15 tens put into groups of 3 tens. There are 5 groups.*  *150 ÷ 30 = 5* | Represent related facts with place value equipment when dividing by unitising.  A picture containing text, clipart  Description automatically generated  *180 is 18 tens.*  *18 tens divided into groups of 3 tens. There are 6 groups.*  *180 ÷ 30 = 6*  A picture containing text, clipart  Description automatically generated  *12 ones divided into groups of 4. There are 3 groups.*  *12 hundreds divided into groups of 4 hundreds. There are 3 groups.*  *1200 ÷ 400 = 3* | Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.  3,000 ÷ 5 = 600  3,000 ÷ 50 = 60  3,000 ÷ 500 = 6  5 × 600 = 3,000  50 × 60 = 3,000  500 × 6 = 3,000 |
| **Dividing up to four digits by a single digit using short division** | Explore grouping using place value equipment.  *268 ÷ 2 = ?*  *There is 1 group of 2 hundreds.*  *There are 3 groups of 2 tens.*  *There are 4 groups of 2 ones.*  *264 ÷ 2 = 134* | Use place value equipment on a place value grid alongside short division.  The model uses grouping.  A sharing model can also be used, although the model would need adapting.  Diagram  Description automatically generated  Lay out the problem as a short division.  *There is 1 group of 4 in 4 tens.*  *There are 2 groups of 4 in 8 ones.*  Work with divisions that require exchange.  A picture containing graphical user interface  Description automatically generated | Use short division for up to 4-digit numbers divided by a single digit.  A picture containing calendar  Description automatically generated  *3,892 ÷ 7 = 556*  Use multiplication to check.  *556 × 7 = ?*  *6 × 7 = 42*  *50 × 7 = 350*  *500 × 7 = 3500*  *3,500 + 350 + 42 = 3,892* |
| **Understanding remainders** | Understand remainders using concrete versions of a problem.  *80 cakes divided into trays of 6.*    *80 cakes in total. They make 13 groups of 6, with 2 remaining.* | Use short division and understand remainders as the last remaining 1s.  Graphical user interface  Description automatically generated | In problem solving contexts, represent divisions including remainders with a bar model.  Timeline  Description automatically generated  *683 = 136 × 5 + 3*  *683 ÷ 5 = 136 r 3* |
| **Dividing decimals by 10, 100 and 1,000** | Understand division by 10 using exchange.    *2 ones are 20 tenths.*  *20 tenths divided by 10 is 2 tenths.* | Represent division using exchange on a place value grid.  Calendar  Description automatically generated  1·5 is 1 one and 5 tenths.  This is equivalent to 10 tenths and 50 hundredths.  10 tenths divided by 10 is 1 tenth.  50 hundredths divided by 10 is 5 hundredths.  1·5 divided by 10 is 1 tenth and 5 hundredths.  1·5 ÷ 10 = 0.15 | Understand the movement of digits on a place value grid.  Table  Description automatically generated  0·85 ÷ 10 = 0·085  Diagram, table  Description automatically generated with medium confidence  8·5 ÷ 100 = 0·085 |
| **Understanding the relationship between fractions and division** | Use sharing to explore the link between fractions and division.  *1 whole shared between 3 people.*  *Each person receives one-third.*  A picture containing clipart  Description automatically generated | Use a bar model and other fraction representations to show the link between fractions and division.  Chart  Description automatically generated | Use the link between division and fractions to calculate divisions. |
| Year 6 | | | |
|  | **Concrete** | **Pictorial** | **Abstract** |
| **Year 6**  **Addition** |  |  |  |
| **Comparing and selecting efficient methods** | Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods. | Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation.  Compare written and mental methods alongside place value representations.  Diagram  Description automatically generated  Use bar model and number line representations to model addition in problem-solving and measure contexts.  Diagram  Description automatically generated | Use column addition where mental methods are not efficient. Recognise common errors with column addition.  *32,145 + 4,302 = ?*  A picture containing text, clock  Description automatically generated  *Which method has been completed accurately?*  *What mistake has been made?*  Column methods are also used for decimal additions where mental methods are not efficient.  A picture containing text, clock  Description automatically generated |
| **Selecting mental methods for larger numbers where appropriate** | Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.    *2,411,301 + 500,000 = ?*  *This would be 5 more counters in the HTh place.*  *So, the total is 2,911,301.*  *2,411,301 + 500,000 = 2,911,301* | Use a bar model to support thinking in addition problems.  *257,000 + 99,000 = ?*  Box and whisker chart  Description automatically generated with low confidence  *I added 100 thousands then subtracted  1 thousand.*  *257 thousands + 100 thousands = 357 thousands*  *257,000 + 100,000 = 357,000*  *357,000 – 1,000 = 356,000*  *So, 257,000 + 99,000 = 356,000* | Use place value and unitising to support mental calculations with larger numbers.  *195,000 + 6,000 = ?*  *195 + 5 + 1 = 201*  *195 thousands + 6 thousands = 201 thousands*  *So, 195,000 + 6,000 = 201,000* |
| **Understanding order of operations in calculations** | Use equipment to model different interpretations of a calculation with more than one operation. Explore different results.  *3 × 5 − 2 = ?*  A picture containing clipart  Description automatically generated | Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations.  Graphical user interface, text, application  Description automatically generated | Understand the correct order of operations in calculations without brackets.  Understand how brackets affect the order of operations in a calculation.  *4 + 6 × 16*  *4 + 96 = 100*  *(4 + 6) × 16*  *10 × 16 = 160* |
| **Year 6**  **Subtraction** |  |  |  |
| **Comparing and selecting efficient methods** | Use counters on a place value grid to represent subtractions of larger numbers.  Diagram  Description automatically generated | Compare subtraction methods alongside place value representations.  A picture containing diagram  Description automatically generated  Diagram  Description automatically generated  Table  Description automatically generated  Use a bar model to represent calculations, including ‘find the difference’ with two bars as comparison.  Diagram  Description automatically generated | Compare and select methods.  Use column subtraction when mental methods are not efficient.  Use two different methods for one calculation as a checking strategy.  A picture containing text, device  Description automatically generated  Use column subtraction for decimal problems, including in the context of measure.  A picture containing text, clock  Description automatically generated |
| **Subtracting mentally with larger numbers** |  | Use a bar model to show how unitising can support mental calculations.  *950,000 − 150,000*  *That is 950 thousands − 150 thousands*  Table  Description automatically generated  *So, the difference is 800 thousands.*  *950,000 − 150,000 = 800,000* | Subtract efficiently from powers of 10.  *10,000 − 500 = ?* |
| **Year 6**  **Multiplication** |  |  |  |
| **Multiplying up to a 4-digit number by a single digit number** | Use equipment to explore multiplications.  Diagram, table  Description automatically generated  *4 groups of 2,345*  *This is a multiplication:*  *4 × 2,345*  *2,345 × 4* | Use place value equipment to compare methods.  Diagram  Description automatically generated  A picture containing chart  Description automatically generated | Understand area model and short multiplication.  Compare and select appropriate methods for specific multiplications.  Table  Description automatically generated |
| **Multiplying up to a 4-digit number by a  2-digit number** |  | Use an area model alongside written multiplication.  Table, calendar  Description automatically generated  Table  Description automatically generated with medium confidence | Use compact column multiplication with understanding of place value at all stages.  Table  Description automatically generated with medium confidence |
| **Using knowledge of factors and partitions to compare methods for multiplications** | Use equipment to understand square numbers and cube numbers.  Shape, arrow  Description automatically generated  *5 × 5 = 52 = 25*  *5 × 5 × 5 = 53 = 25 × 5 = 125* | Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.  Diagram  Description automatically generated  Represent and compare methods using a bar model. | Use a known fact to generate families of related facts.  Diagram  Description automatically generated  Use factors to calculate efficiently.  *15 × 16*  *= 3 × 5 × 2 × 8*  *= 3 × 8 × 2 × 5*  *= 24 × 10*  *= 240* |
| **Multiplying by 10, 100 and 1,000** | Use place value equipment to explore exchange in decimal multiplication.  Diagram, table  Description automatically generated  *0·3 × 10 = ?*  *0·3 is 3 tenths.*  *10 × 3 tenths are 30 tenths.*  *30 tenths are equivalent to 3 ones.* | Understand how the exchange affects decimal numbers on a place value grid.  Diagram  Description automatically generated  Table  Description automatically generated with low confidence  0·3 × 10 = 3 | Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000.  *8 × 100 = 800*  *8 × 300 = 800 × 3*  *= 2,400*  *2·5 × 10 = 25*  *2·5 × 20 = 2·5 × 10 × 2*  *= 50* |
| **Multiplying decimals** | Explore decimal multiplications using place value equipment and in the context of measures.  A picture containing text, clipart  Description automatically generated  *3 groups of 4 tenths is 12 tenths.*  *4 groups of 3 tenths is 12 tenths.*  Diagram  Description automatically generated  *4 × 1 cm = 4 cm*  *4 × 0*·*3 cm = 1.2 cm*  *4 × 1*·*3 = 4 + 1*·*2 = 5*·*2 cm* | Represent calculations on a place value grid.  Table  Description automatically generated  Understand the link between multiplying decimals and repeated addition.  Diagram  Description automatically generated | Use known facts to multiply decimals.  4 × 3 = 12  4 × 0·3 = 1·2  4 × 0·03 = 0·12  20 × 5 = 100  20 × 0·5 = 10  20 × 0·05 = 1  Find families of facts from a known multiplication.  I know that 18 × 4 = 72.  This can help me work out:  1·8 × 4 = ?  18 × 0·4 = ?  180 × 0·4 = ?  18 × 0·04 = ?  Use a place value grid to understand the effects of multiplying decimals.  Calendar  Description automatically generated |
| **Year 6**  **Division** |  |  |  |
| **Understanding factors** | Use equipment to explore different factors of a number.  A picture containing text, clipart  Description automatically generated  *4 is a factor of 24 but is not a factor of 30.* | Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.  A screenshot of a computer  Description automatically generated with medium confidence | Recognise and know primes up to 100.  Understand that 2 is the only even prime, and that 1 is not a prime number.  A picture containing text, shoji, crossword puzzle  Description automatically generated |
| **Dividing by a single digit** | Use equipment to make groups from a total.  Background pattern  Description automatically generated  *There are 78 in total.*  *There are 6 groups of 13.*  *There are 13 groups of 6.* | Diagram  Description automatically generated | Use short division to divide by a single digit.  A picture containing text, clock  Description automatically generated  Use an area model to link multiplication and division.  Table  Description automatically generated with low confidence |
| **Dividing by a 2-digit number using factors** | Understand that division by factors can be used when dividing by a number that is not prime. | Use factors and repeated division.  *1,260 ÷ 14 = ?*  Graphical user interface, application  Description automatically generated with medium confidence  *1,260 ÷ 2 = 630*  *630 ÷ 7 = 90*  *1,260 ÷ 14 = 90* | Use factors and repeated division where appropriate.  *2,100 ÷ 12 = ?*  Shape  Description automatically generated with medium confidence |
| **Dividing by a 2-digit number using long division** | Use equipment to build numbers from groups.  A picture containing bar chart  Description automatically generated  *182 divided into groups of 13.*  *There are 14 groups.* | Use an area model alongside written division to model the process.  *377 ÷ 13 = ?*  A picture containing chart  Description automatically generated  *377 ÷ 13 = 29* | Use long division where factors are not useful (for example, when dividing by a  2-digit prime number).  Write the required multiples to support the division process.  *377 ÷ 13 = ?*    A picture containing text, clock  Description automatically generated  *377 ÷ 13 = 29*  A slightly different layout may be used, with the division completed above rather than at the side.  A screenshot of a calculator  Description automatically generated with medium confidence  Divisions with a remainder explored in problem-solving contexts. |
| **Dividing by 10, 100 and 1,000** | Use place value equipment to explore division as exchange.  Diagram  Description automatically generated  *0·2 is 2 tenths.*  *2 tenths is equivalent to 20 hundredths.*  *20 hundredths divided by 10 is 2 hundredths.* | Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.  Graphical user interface  Description automatically generated with low confidence  Understand how to divide using division by 10, 100 and 1,000.  12 ÷ 20 = ?  Diagram  Description automatically generated with medium confidence | Use knowledge of factors to divide by multiples of 10, 100 and 1,000.  Graphical user interface, application  Description automatically generated  *40 ÷ 5 = 8*  *8 ÷ 10 = 0·8*  *So, 40 ÷ 50 = 0·8* |
| **Dividing decimals** | Use place value equipment to explore division of decimals.  A picture containing text, clipart  Description automatically generated  *8 tenths divided into 4 groups. 2 tenths in each group.* | Use a bar model to represent divisions.  Table  Description automatically generated | Use short division to divide decimals with up to 2 decimal places.  A picture containing text, clock  Description automatically generated |